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Density-Corrected Density Functional Theory for Solids

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Abstract

Density-corrected density functional theory (DC-DFT) considers whether self-consistent densities yield optimal energetics in Kohn-Sham calculations. With considerable success in molecular calculations, we here apply DC-DFT to solid-state calculations with Hartree-Fock (HF) densities. We resolve a known anomaly: that dispersion corrections can worsen results as one climbs Jacob's ladder. This is illustrated for simple covalent solids, such as Si. The relative energetics of phases of ice are also much improved with HF densities, as is CO absorption on NaCl, while graphite interlayer binding is insensitive to its density.

Density-Corrected Density Functional Theory for Solids

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Density-corrected density functional theory (DC-DFT) considers whether self-consistent densities yield optimal energetics in Kohn-Sham calculations. With considerable success in molecular calculations, we here apply DC-DFT to solid-state calculations with Hartree-Fock (HF) densities. We resolve a known anomaly: that dispersion corrections can worsen results as one climbs Jacob’s ladder. This is illustrated for simple covalent solids, such as Si. The relative energetics of phases of ice are also much improved with HF densities, as is CO adsorption on NaCl, while graphite interlayer binding is insensitive to its density.

With the advent of high-throughput materials searches[1, 2] and machine-learned interatomic potentials[3–6], density functional theory (DFT), long a cornerstone of electronic structure theory[7], has become even more central to modern condensed-matter physics[8, 9] and materials science[10]. The predictive power of such calculations is commonly attributed to the accuracy of approximate exchange–correlation (XC) functionals,[11] implicitly assuming that the self-consistent electron density obtained from a given functional is sufficiently accurate. Well-known deficiencies include self-interaction and strong-correlation errors,[12–15] motivating extensive efforts to develop improved approximations along Jacob’s ladder.[16–18]

However, not all failures of Kohn–Sham calculations can be attributed solely to the XC functional. The total energy error can be decomposed into functional and density-driven contributions, the latter arising from inaccuracies in the self-consistent density. This perspective underlies density-corrected DFT (DC-DFT),[19] which has been extensively studied in molecular systems. While most systems exhibit small density-driven errors (DDEs), those that do not can be substantially improved by evaluating functionals on alternative densities, and a wide range of chemical properties have been shown to be density-sensitive.[20–27] While this framework is well established in molecular systems, its implications for condensed-phase calculations remain less explored.

In pioneering work on surfaces, Patra *et al.*[28] applied PBE+U densities to the CO/Pt(111) puzzle[29], suggesting that density-driven self-interaction errors can dominate adsorption energetics and site preferences. Related studies have reported similar effects in molecule–surface systems[30, 31], transition-metal oxides[32], simulations of water[33], and aqueous radicals[34]. However, for condensed-phase systems, existing studies remain limited to specific cases, and a general understanding of DDEs across diverse bonding environments is still lacking. In particular, their role in the inconsistencies observed in standard solid-state calculations has not been systematically established. One manifestation of this problem is a long-standing paradox in solid-state DFT: dispersion in-

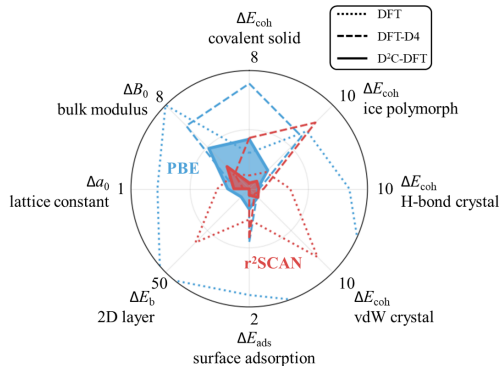


Figure 1. Comparison of pure DFT, dispersion-corrected DFT (DFT-D4), and density- and dispersion-corrected DFT (D²C-DFT) across main-group non-metallic solids properties, grouped by bonding character. Errors are normalized to characteristic reference scales. Cohesive and adsorption energies (ΔE_{coh} , ΔE_{ads}) are reported in kcal/mol, graphite binding energies (ΔE_{b}) in meV/atom, and structural properties (lattice constants and bulk moduli) in %. Dispersion corrections produce nonuniform changes in accuracy across systems, an inconsistency that is resolved with the use of the HF density.

teractions are known to be significant[35, 36], yet adding them to semilocal functionals does not lead to consistent improvement in accuracy.

Figure 1 provides a representative overview of this trend across main-group non-metallic solids. A clear pattern emerges: the effect of dispersion corrections varies widely across systems, with no consistent improvement in agreement with reference data. This pattern cannot be explained by dispersion interactions alone and instead points to a more general source of error in condensed-phase DFT.

Here we show that this inconsistency correlates with the density sensitivity, whose magnitude varies with bonding character and can be significant even in systems traditionally regarded as well described by semilocal functionals. When density sensitivities are significant, the total energy can already be biased at the level of the self-consistent density, such that additional contributions, including dispersion, may amplify existing errors

rather than improve agreement. By contrast, evaluating functionals on the HF density in these systems reduces these inconsistencies and restores physically consistent energetic trends. These results establish density sensitivity as a central factor governing the accuracy of DFT in condensed-phase systems.

Next, we briefly outline the theoretical framework underlying DDEs. For a given external potential $v(\mathbf{r})$, the total energy error arising from a self-consistent Kohn–Sham DFT[37] calculation can be decomposed as

$$\Delta E = \tilde{E}[\tilde{n}] - E[n] = (\tilde{E}_{\text{xc}}[n] - E_{\text{xc}}[n]) + (\tilde{E}[\tilde{n}] - \tilde{E}[n]), \quad (1)$$

where the first term is the functional error and the second is the DDE. The functional error reflects the intrinsic limitation of the approximate XC functional even when evaluated on the exact density, whereas the DDE arises from inaccuracies in the self-consistent density.

This separation underlies density-corrected DFT (DC-DFT), in which evaluating the functional on an alternative density can reduce energetic errors without modifying the functional when DDEs are significant.[38–41] In practice, for molecular calculations, a simple and widely used approach is to evaluate the XC functional on the HF density, which can yield improved energies for systems with large DDEs.[42, 43] However, in some problems, HF densities reduce errors by more than the DDE[44–47], so the success of HF-DFT[48, 49] remains to be understood.

A key diagnostic for identifying regimes with significant DDEs is the density sensitivity,[50] defined as

$$\tilde{S} = \left| \tilde{E}[n^{\text{HF}}] - \tilde{E}[n^{\text{LDA}}] \right|. \quad (2)$$

Large values of \tilde{S} indicate that the approximate functional is highly sensitive to the density, such that errors in the self-consistent density can lead to large changes in the total energy, which signals a substantial DDE. Conversely, when \tilde{S} is small, the energy is relatively insensitive to the density, and DDEs are expected to be small.

Inaccuracies in the self-consistent density can therefore lead to significant biases in the total energy and give rise to inconsistent energetic predictions. A prominent manifestation of this effect is that dispersion corrections may fail to improve agreement with reference energetics when evaluated on an inaccurate density and can even worsen it.

By contrast, when evaluated on the HF density, particularly in density-sensitive cases, these inconsistencies are largely removed, and dispersion corrections restore physically consistent energetics. This motivates the density- and dispersion-corrected DFT (D²C-DFT) framework,[52, 53] in which dispersion corrections are evaluated on the HF density, while their parameters are determined so as to avoid contamination from DDEs. Recent progress in KS inversion for solids[54] further underscores the importance of the electron density itself in determining electronic properties, including band gaps.

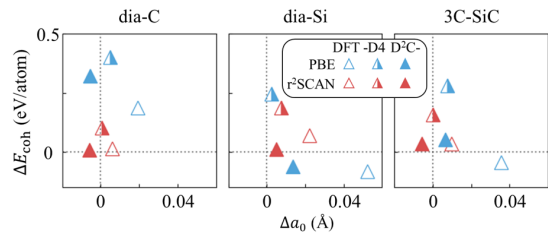


Figure 2. Effects of density and dispersion corrections in prototypical covalent solids. Errors in cohesive energy (ΔE_{coh}) and lattice constant (Δa_0) relative to reference values[51] are shown. The impact of dispersion corrections varies markedly with the underlying density, suggesting that energetic accuracy is governed by DDEs, as evidenced by the large density sensitivities (Table S3), even in covalent solids.

Before presenting the results, we briefly summarize the computational framework. We focus on representative semilocal generalized gradient approximation (GGA) and meta-GGA functionals, PBE[55] and r²SCAN[56], evaluated in three forms: self-consistent DFT, dispersion-corrected DFT (DFT-D4), and D²C-DFT. Dispersion interactions are treated using the D4 method.[57, 58] All calculations are well converged with respect to basis set, computational settings, and dispersion parameters; further details and validation are provided in the Supplemental Material[59], including Fig. S1, Tables S1–S2, and Refs.[60–64] therein.

We find that energetic predictions in DFT for main-group non-metallic solids are sensitive to the choice of density; and that the extent of this sensitivity varies across bonding regimes. As summarized in Fig. 1, dispersion corrections produce no consistent improvement in accuracy, indicating the presence of an additional source of error. This behavior is captured by the density sensitivity, suggesting contributions from DDEs.

Covalent solids— We first examine prototypical covalent solids: diamond C (dia-C), Si (dia-Si), and zincblende SiC (3C-SiC), where DDEs are commonly assumed to be negligible. To quantify energetic accuracy, we consider the cohesive energy,

$$E_{\text{coh}} = E_{\text{gas}} - E_{\text{crys}}, \quad (3)$$

where E_{crys} and E_{gas} are the crystal and isolated constituent energies, respectively, expressed per atom (or per molecule for molecular crystals).

Dispersion corrections are known to improve lattice constants but often worsen cohesive energies.[65, 66] Figure 2 shows this trend for representative covalent solids. This long-standing inconsistency arises in density-sensitive regimes, as additional attractive dispersion contributions amplify pre-existing energetic biases.

This apparent trade-off is not specific to DFT-D4 (see PBE+MBD@rSCS and r²SCAN+rVV10 in Fig. S2). Consistently, D²C-DFT improves energetic predictions and alleviates the trade-off between lattice constants and cohesive energies.

Table I. Mean error (ME) and mean absolute error (MAE) in cohesive energies for the ICE7 and X23 datasets in kcal/mol. Experimental reference values are from Refs.[67] and [68]. The X23 dataset is divided into hydrogen-bond (H-bond), mixed (Mix), and van der Waals (vdW) subsets (number of systems in parentheses). The lowest MAE in each category is shown in bold. Density-corrected approaches improve accuracy in density-sensitive systems (*e.g.*, hydrogen-bonded) while maintaining comparable performance in density-insensitive cases.

kcal/mol		PBE			r ² SCAN		
		D ² C-	-D4	DFT	D ² C-	-D4	DFT
ICE7	ME	0.3	1.3	-1.3	0.2	1.6	0.4
	MAE	0.4	1.3	1.4	0.2	1.6	0.4
total (23)	ME	0.6	-0.4	-12.2	-0.6	0.1	-6.5
	MAE	0.9	0.9	12.2	1.0	0.8	6.5
H-bond (8)	ME	0.1	0.2	-8.5	-0.2	1.1	-3.5
	MAE	0.7	0.9	8.5	0.8	1.2	3.5
Mix (4)	ME	0.6	-0.1	-12.4	-0.8	0.0	-6.6
	MAE	0.8	0.4	12.4	0.8	0.4	6.6
vdW (11)	ME	0.9	-1.0	-14.9	-0.9	-0.7	-8.7
	MAE	1.1	1.1	14.9	1.1	0.7	8.7

Table S3 shows that density sensitivities are irrelevant at the local density approximation (LDA) level but become significant for more accurate GGAs and meta-GGAs, in some cases comparable to or exceeding the total self-consistent DFT error. This could suggest that DDEs are not negligible even in prototypical covalent solids.

For the bulk modulus, density and dispersion corrections modify the values for both PBE and r²SCAN, typically by about 2-4% (Table S4). Analysis of the equation-of-state curves[69, 70] in Table S5 further indicates that the dominant contribution to the overall discrepancy originates from cohesive energy errors, whereas higher-order volume terms such as the bulk modulus play only a minor role.

Molecular crystals— We next examine systems where DDEs are expected to be more pronounced, namely molecular crystals stabilized by hydrogen-bonds and dispersion interactions. The ICE7 dataset, comprising seven ice polymorphs with experimental references,[67] provide a stringent test, with cohesive energy differences of only ~ 1 kcal/mol.[71, 72] As shown in Table I, dispersion corrections on self-consistent densities often overcorrect functional errors, leading to little improvement compared to pure DFT. D²C- systematically reduces the mean absolute error to less than $\frac{1}{2}$ kcal/mol. As shown in Fig. 3, PBE underbinds while r²SCAN slightly overbinds, and dispersion corrections improve relative ordering but often worsen absolute energies. D²C-PBE substantially mitigates this inconsistency.

To extend beyond density-sensitive cases, we consider the X23 dataset[73–77] spanning hydrogen-bonded, mixed, and van der Waals crystals. Table I shows

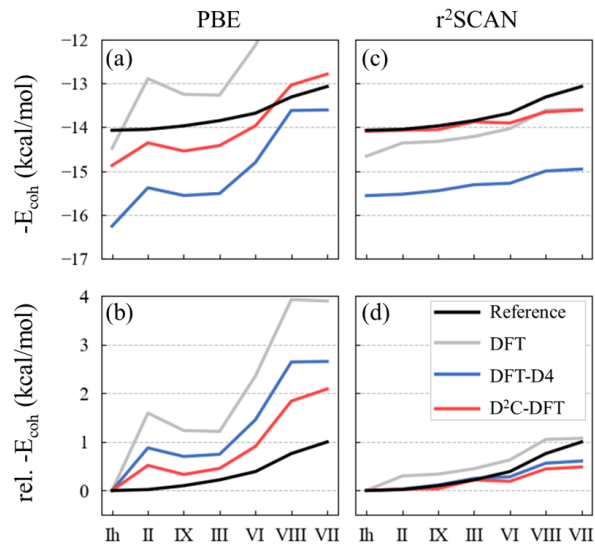


Figure 3. Cohesive energies of seven ice polymorphs (ICE7). Density correction restores agreement with experiment, which commensurate with the density sensitivities of hydrogen-bonded systems.

that the energetic predictions for hydrogen-bonded systems depend strongly on the choice of density, whereas dispersion-dominated systems are largely insensitive and already well described by dispersion-corrected DFT. Comparison with recent diffusion Monte Carlo results[78] in Table S6 confirms that these qualitative trends remain unchanged.

These trends can be understood in terms of the density sensitivity (Eq. 2). As shown in Fig. 4, systems separate according to this metric. Hydrogen-bonded crystals exhibit large values, suggesting substantial DDEs, whereas dispersion-dominated systems show minimal sensitivity, indicating weak density dependence. Importantly, the magnitude of density sensitivity is comparable to that of dispersion contributions, placing both effects on the same energetic scale.

Surface adsorption— We further test this framework in CO adsorption on NaCl(100)[79–81], where electrostatic interactions are expected to introduce intermediate DDEs. As shown in Fig. 5, dispersion-corrected DFT overestimates adsorption energies, whereas density correction systematically reduces overbinding. These results indicate that energetic predictions in surfaces depend sensitively on the choice of density.

Density-insensitive limit— Finally, graphite interlayer binding[82] represents a density-insensitive limit. The negligible density sensitivity suggests that DDEs are small and that binding is dominated by dispersion interactions (see Figs. S3-S4).

In summary, our results establish DDEs as the missing piece behind the nonuniform impact of dispersion corrections in condensed-phase DFT, as reflected in the density sensitivity and confirmed by the systematic improvement with D²C-DFT. In density-sensitive regimes, dispersion

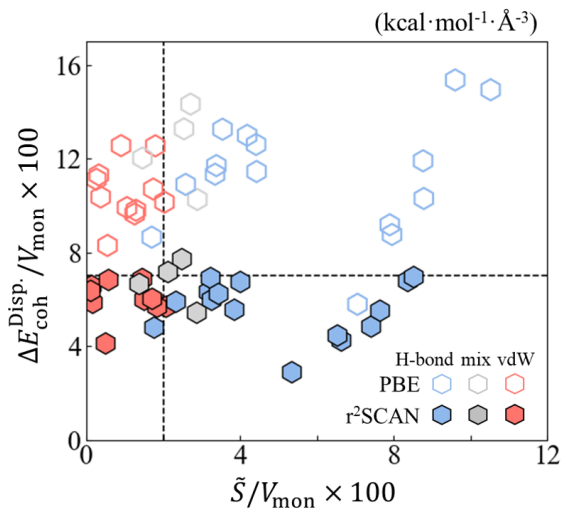


Figure 4. Density sensitivity \tilde{S} versus dispersion contributions $\Delta E_{\text{coh}}^{\text{Disp.}}$ in molecular crystals (ICE7 and X23), with both quantities normalized by the monomer volume V_{mon} . Large density sensitivity signals regimes where DDEs dominate energetic errors, whereas small sensitivity indicates weak dependence on the density. The separation of systems according to bonding character is consistent across functionals, indicating that the dominant error regime is determined by bonding physics rather than by the choice of functional.

corrections can worsen energetic accuracy by reinforcing pre-existing errors, whereas D²C-DFT can restore consistent accuracy. Density sensitivity thus serves as a practical indicator for identifying regimes where density correction is most beneficial.

Even in prototypical covalent solids, where density errors are commonly assumed negligible, density sensitivities can become comparable to the total self-consistent DFT error. Across molecular crystals, surface adsorption, and layered materials, this framework consistently explains when standard approximations succeed or fail, providing a unified description of binding across bulk, molecular, and interfacial environments.

Importantly, these results do not imply that HF densities are universally more accurate or should be adopted in all solid-state calculations. They would be inappropriate for metals, for example. But where appropriate in density-sensitive regimes, the D²C-DFT framework consistently improves energetic predictions, suggesting that it mitigates density-driven contributions to the error. An alternative density worth exploring would be that of RPA[83, 84].

More broadly, our findings highlight the central role of the electron density in determining energetic accuracy and suggest that controlling DDEs will be essential for achieving consistent predictive performance in large-scale materials simulations. Challenges remain, including the scarcity of benchmark-quality reference data for extended systems and the cost of obtaining HF densities for large-scale calculations. Ongoing advances

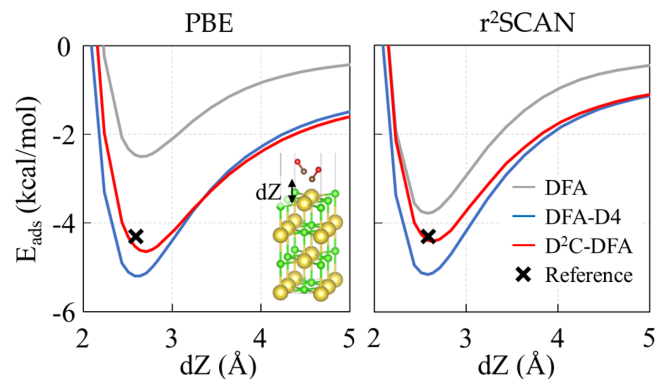


Figure 5. Potential energy surfaces for CO adsorption on NaCl(100). Dispersion corrections overbind adsorption energies, whereas D²C-DFT restores agreement with experiment. The same framework consistently describes binding across bulk, molecular, and surface environments, highlighting the generality of DDEs in governing energetic accuracy.

in high-level benchmarks and electronic-structure methods are expected to further clarify and extend the role of DC-DFT in condensed-phase systems.

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